



# REBOUND 2024: xGEO NUMERICAL INTEGRATOR ANALYSIS AND MANEUVER DETECTION

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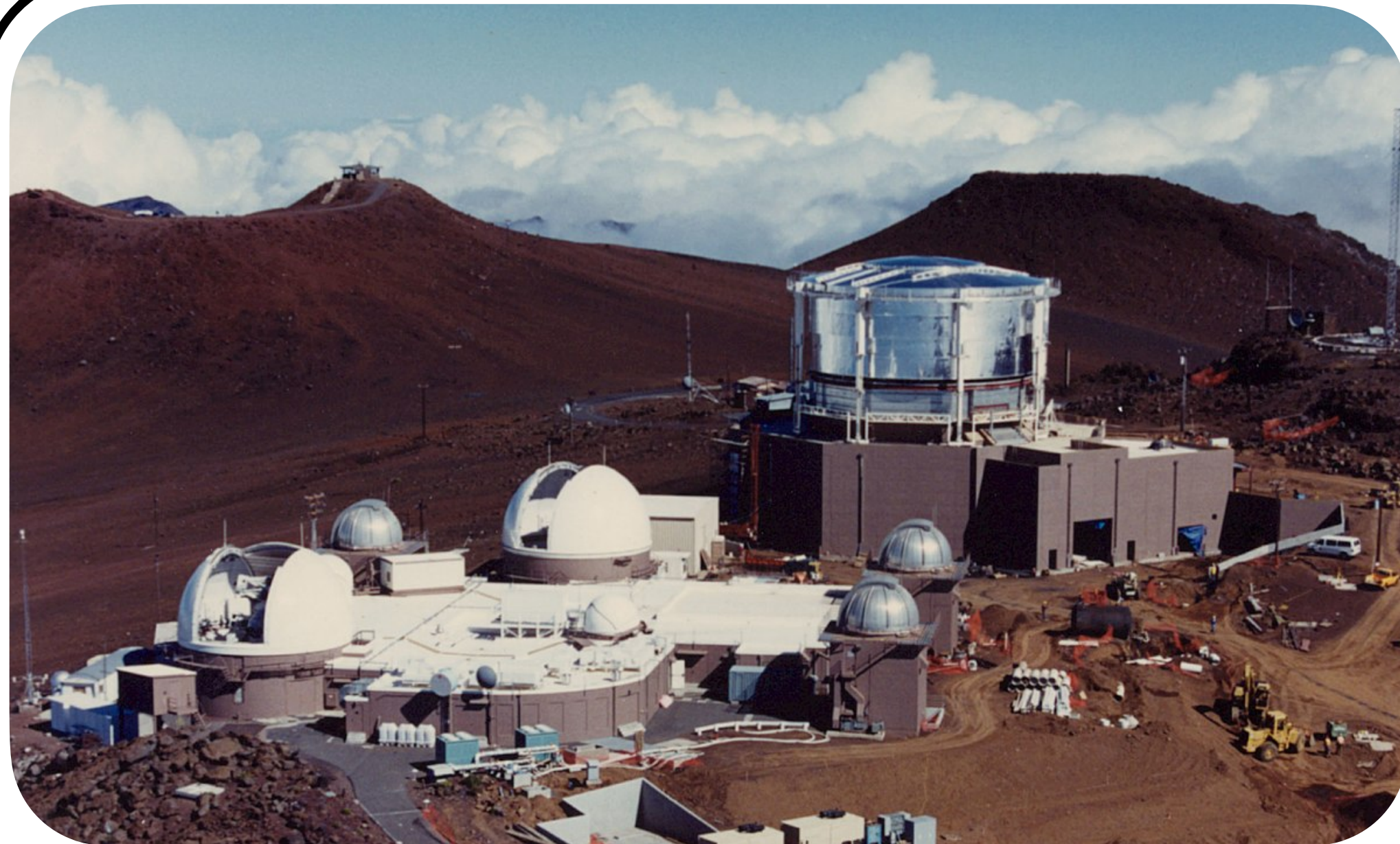


## Optical detection of suboptimal objects in suboptimal regimes



### 15th Space Surveillance Squadron (SPSS)

- Space domain awareness (SDA), space situational awareness (SSA), rendezvous proximity operations (RPOs), astronomy, spectroscopy, optimal trajectory control, near-Earth and **deep-space object detection**
- **Overarching objective:** Utilization of highly advanced tracking optics (including DoD's largest optical telescope) for tracking and imaging deep-space (possibly uncooperative) satellites



Mt. Haleakala, AEOS telescope (3.6 m aperture)

### Suboptimal Objects

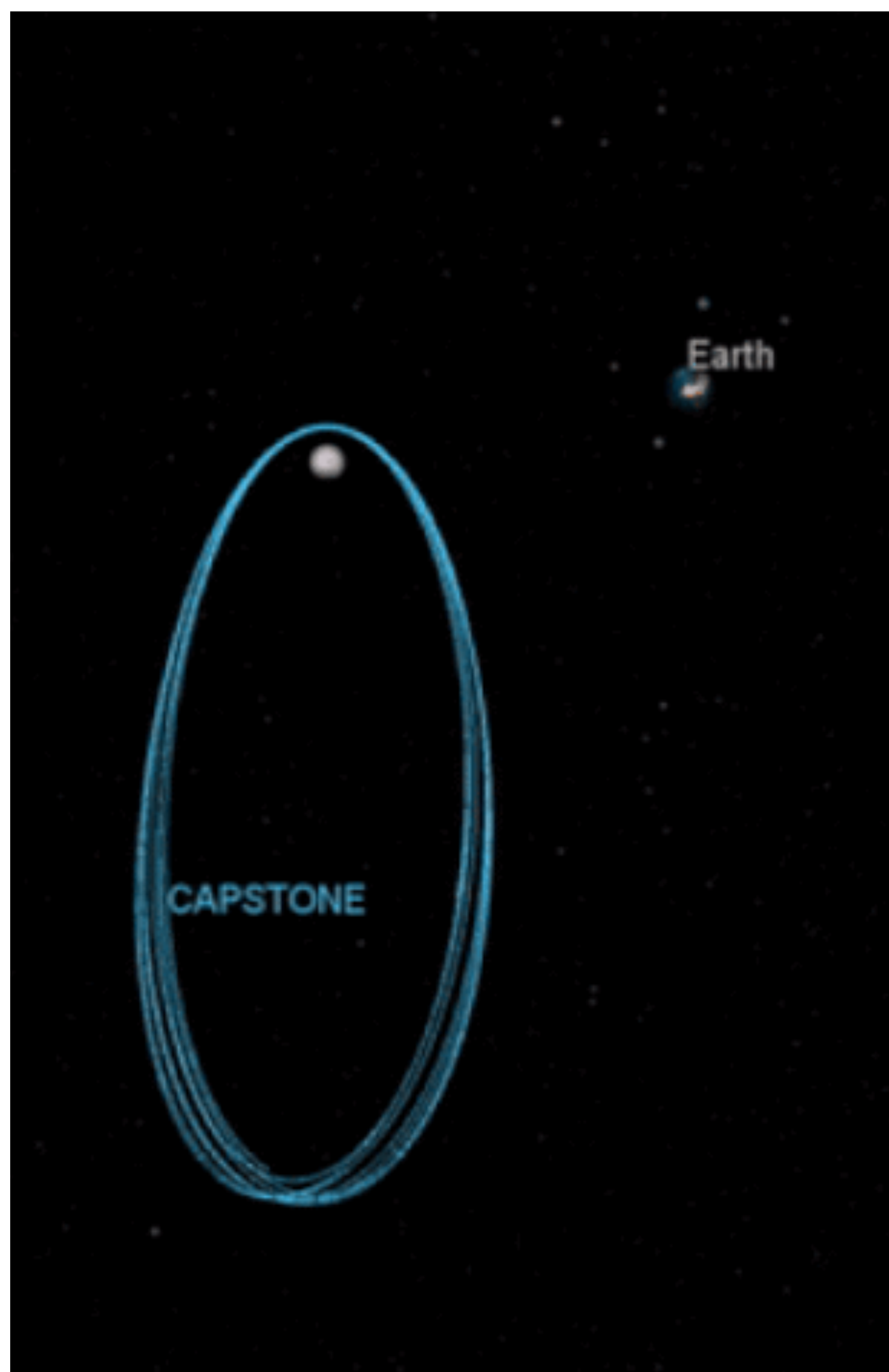
- Miniaturization of satellite technology (CubeSats) has increased the difficulty of tracking and imaging objects with smaller apparent magnitudes

### Suboptimal Regimes

- xGEO objects are governed by dynamics that are less predictable than LEO or GEO objects
- Detection of lunar orbiters require telescopes to point closer to the Moon, decreasing signal-to-noise ratio and shortening viable observation periods



# CAPSTONE



## Motivation

of suboptimal objects in suboptimal

### Surveillance Squadron (SPSS)

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**ection**

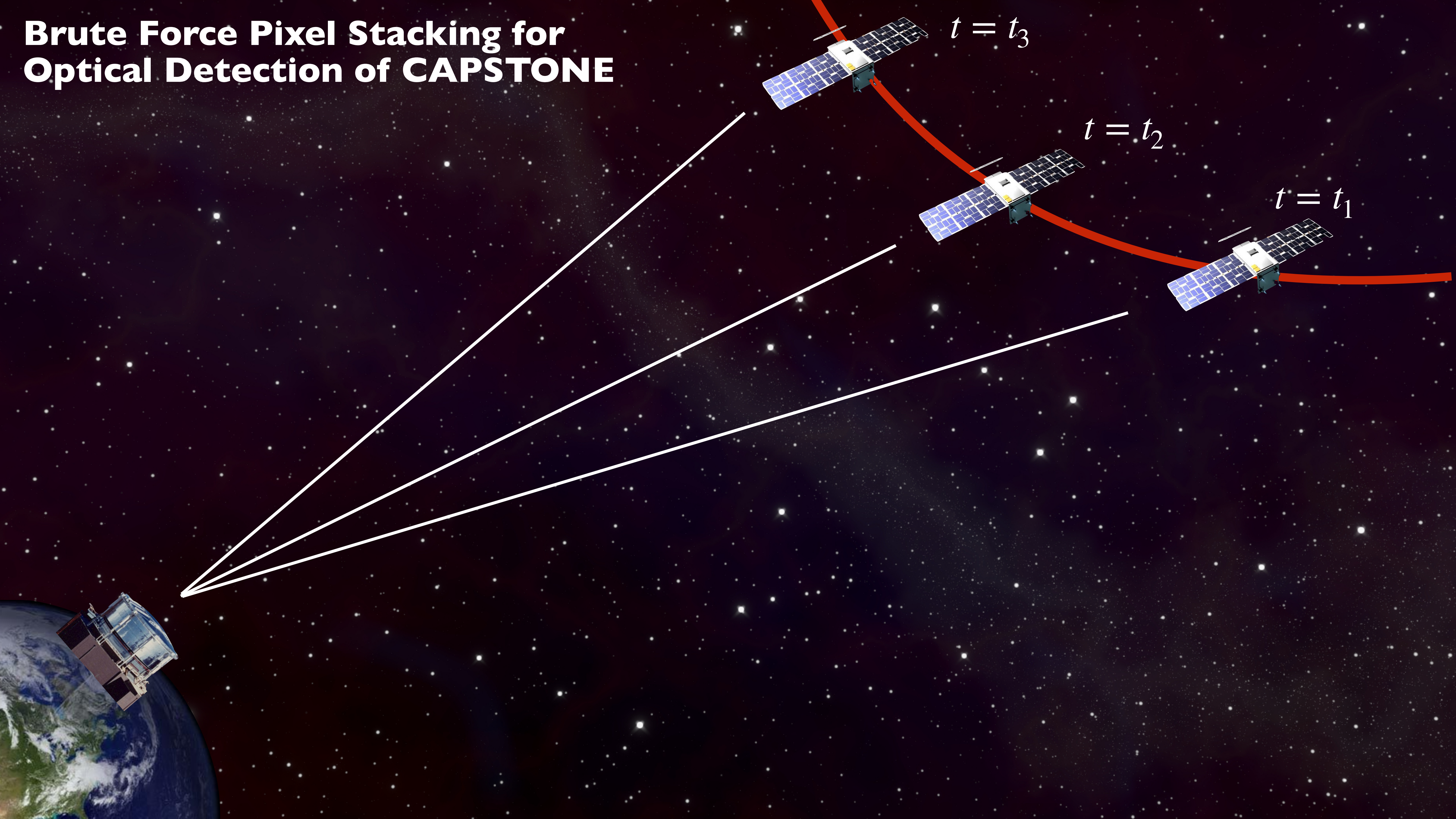
**ective:** Utilization of highly advanced tracking optics (including DoD's scope) for tracking and imaging deep-space (possibly uncooperative) satellites

- **12U CubeSat traveling in a near-rectilinear halo orbit (NRHO) about the  $L_2$  Earth-Moon libration point**
  - Miniaturization of satellite technology (CubeSats) has
- **Launched 28 Jun. 2022, inserted into NRHO on 14 Nov. 2022**
  - objects with smaller apparent magnitudes
- **Period of  $\sim 6.5$  days, periselene altitude:  $\sim 1,500$  km, aposelene altitude:  $\sim 70,000$  km**
  - NEO objects are governed by dynamics that are less predictable than LEO or GEO objects
- **Operated by Advanced Space, ephermides available on JPL Horizons**
  - Detection of lunar orbiters require telescopes to point closer to the Moon, decreasing signal-to-noise ratio and shortening viable observation periods



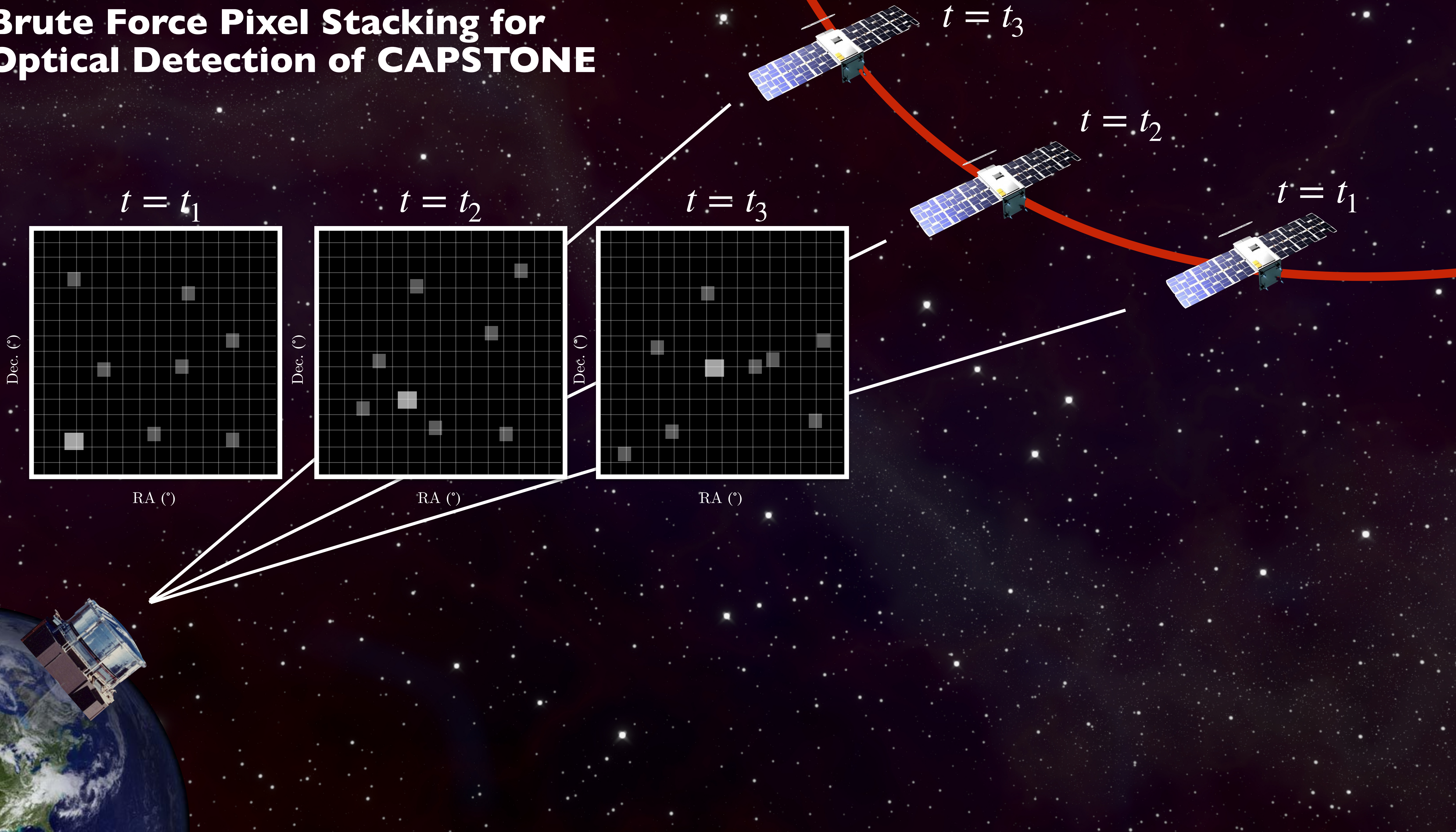


# Brute Force Pixel Stacking for Optical Detection of CAPSTONE



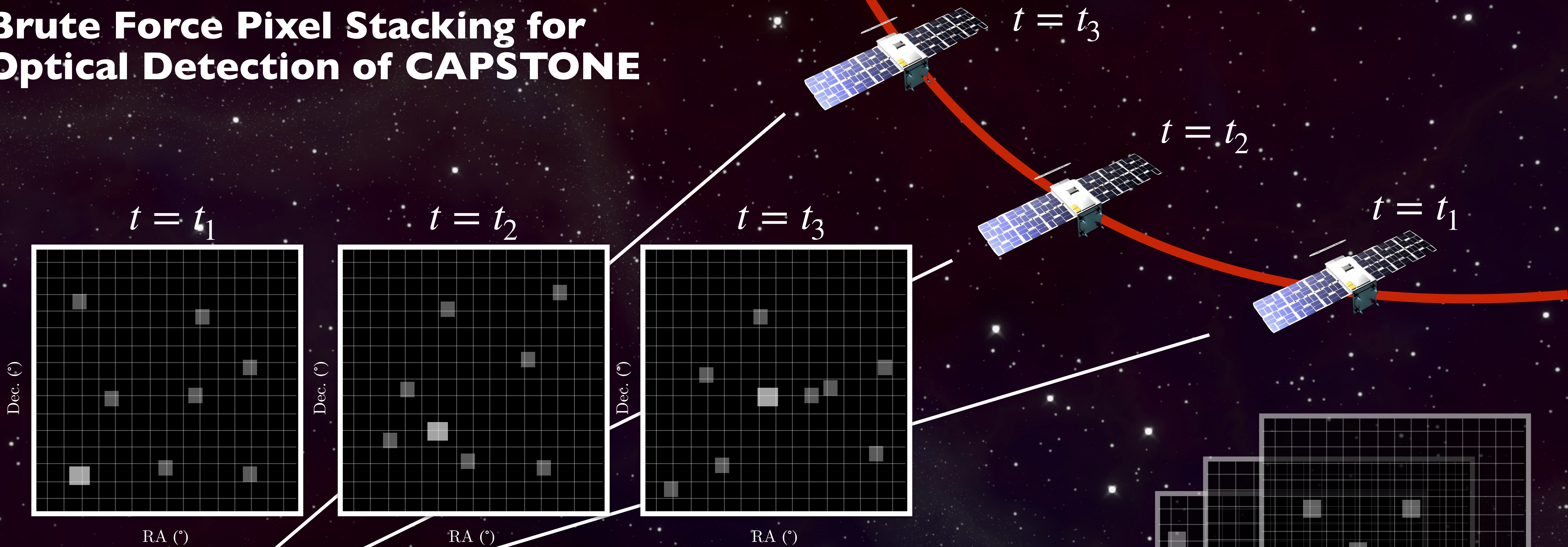


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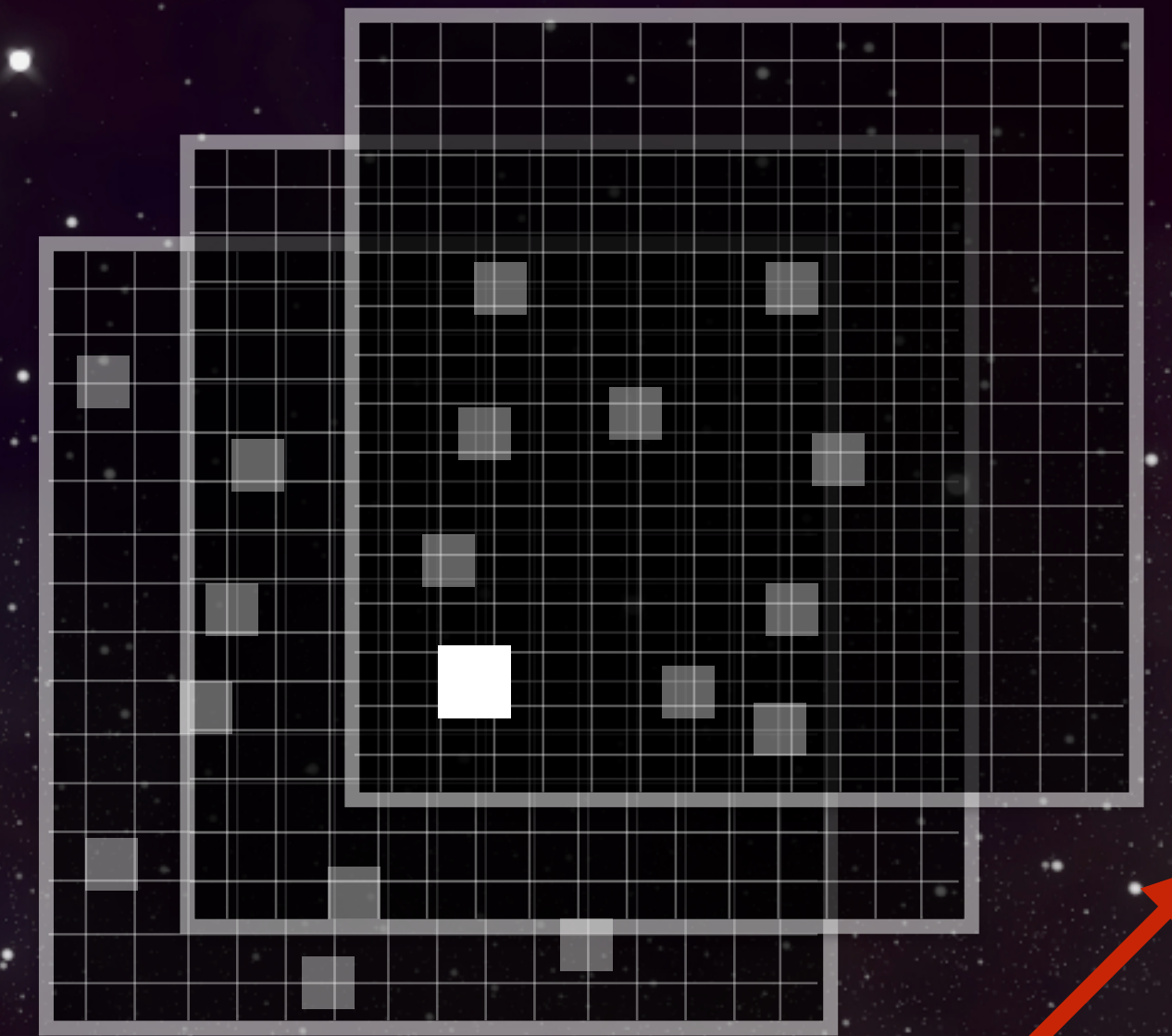


# Brute Force Pixel Stacking for Optical Detection of CAPSTONE



## Shift detections by ephemeris

**Fundamental Question:** Are state-of-the-art numerical integrators accurate enough to be utilized by optical detection methods in the xGEO regime when the ephemeris is unavailable? If so, what is the limit of this accuracy with respect to the length of the propagation period?

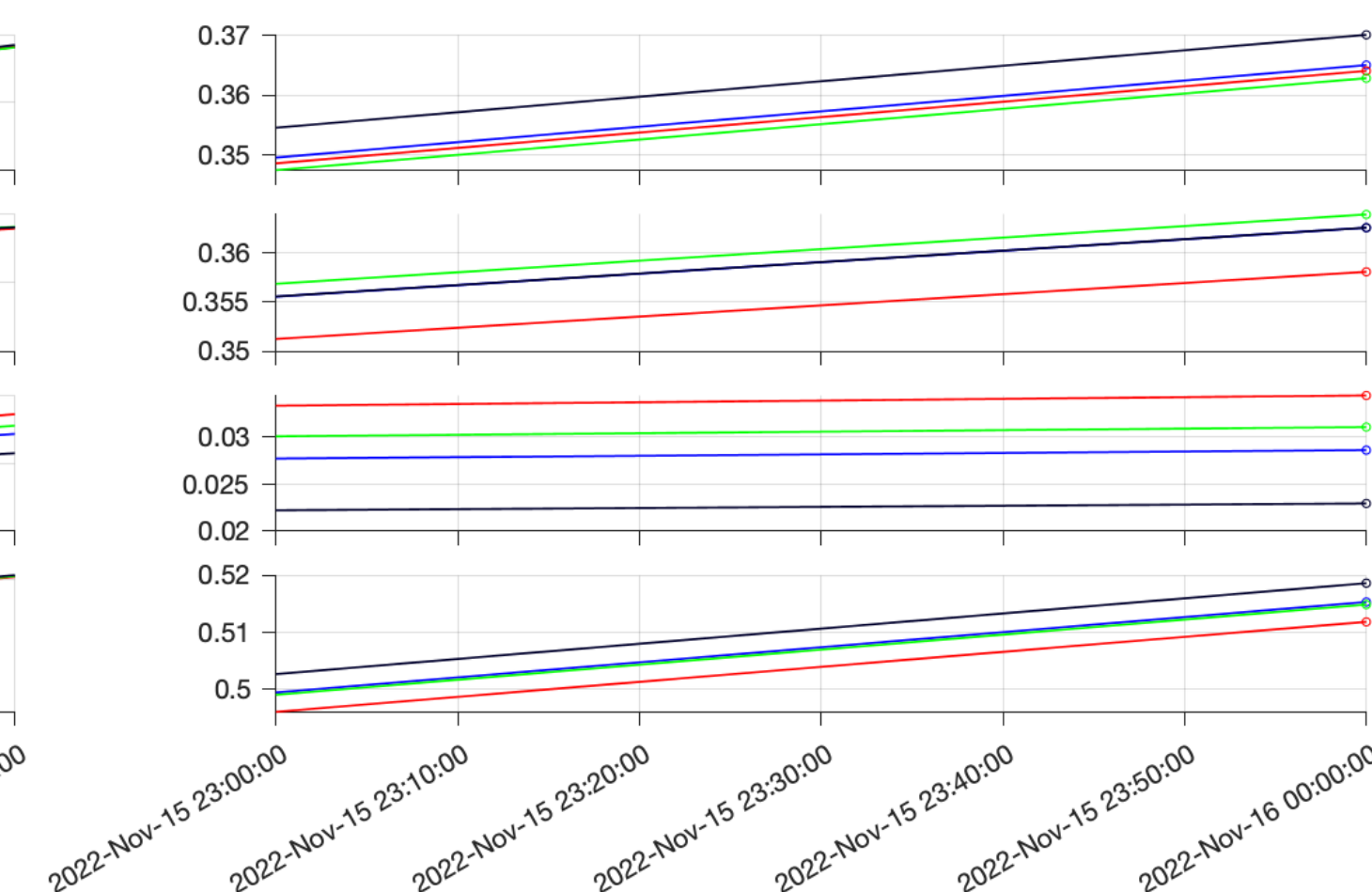
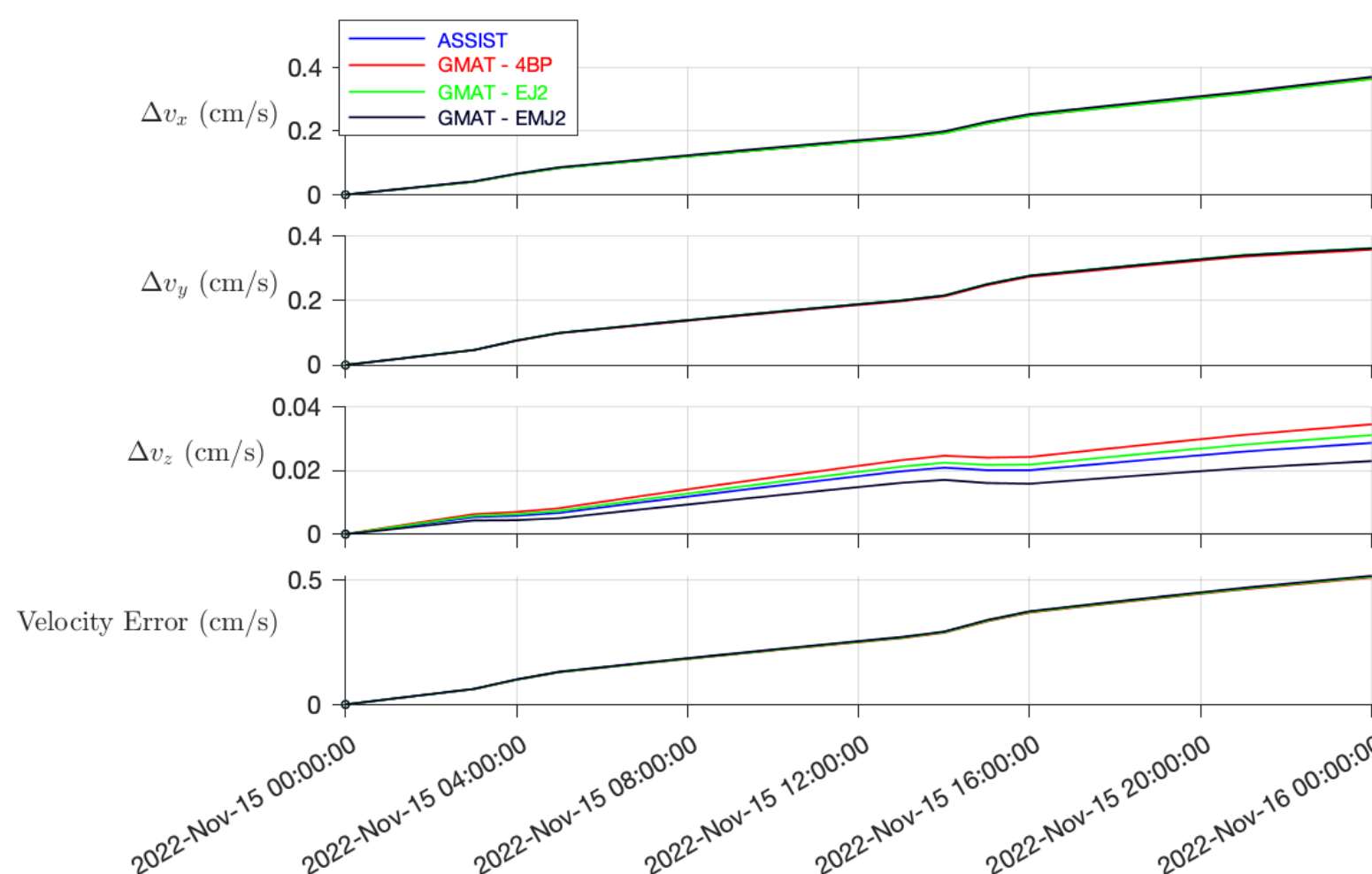
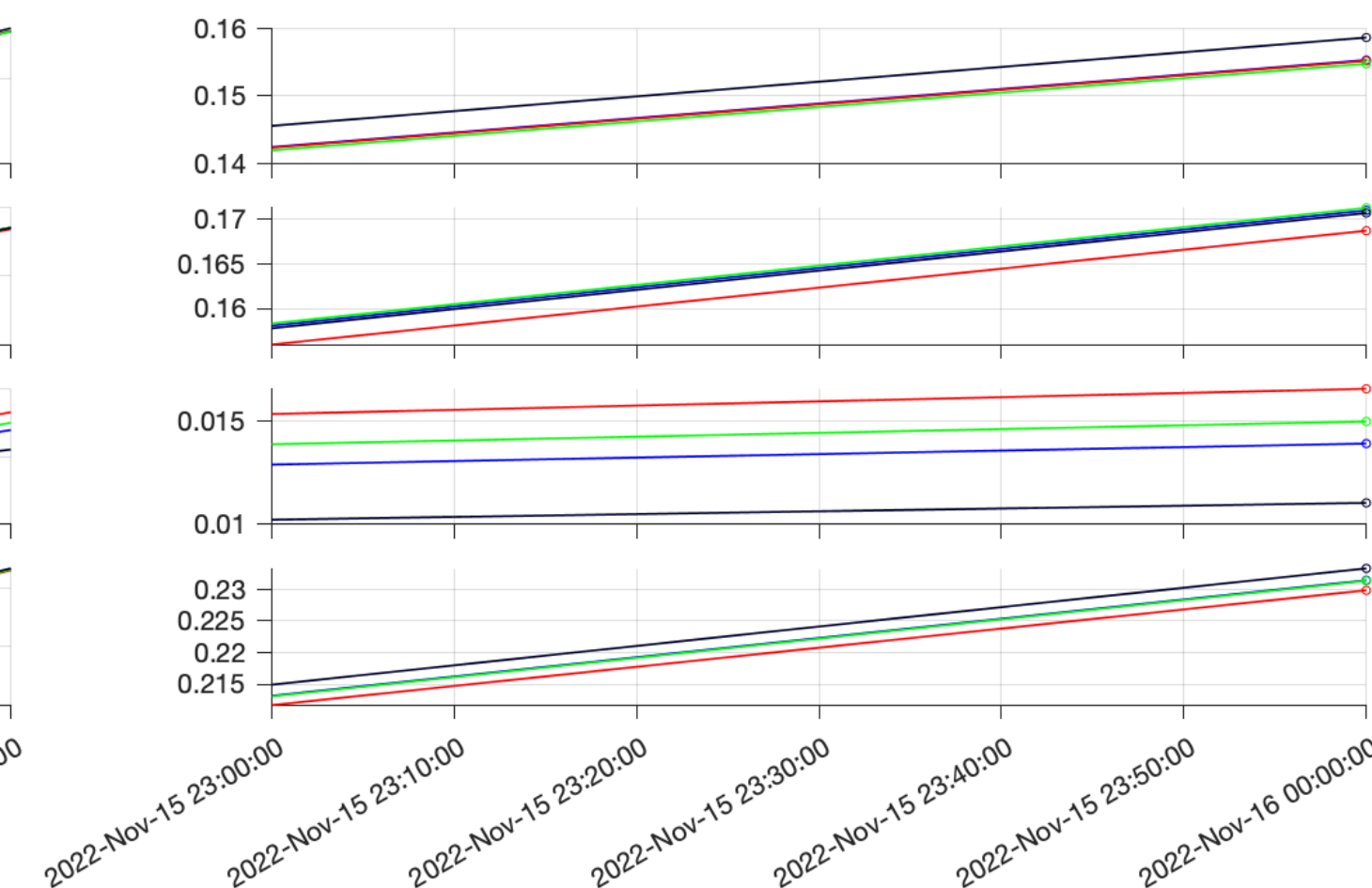
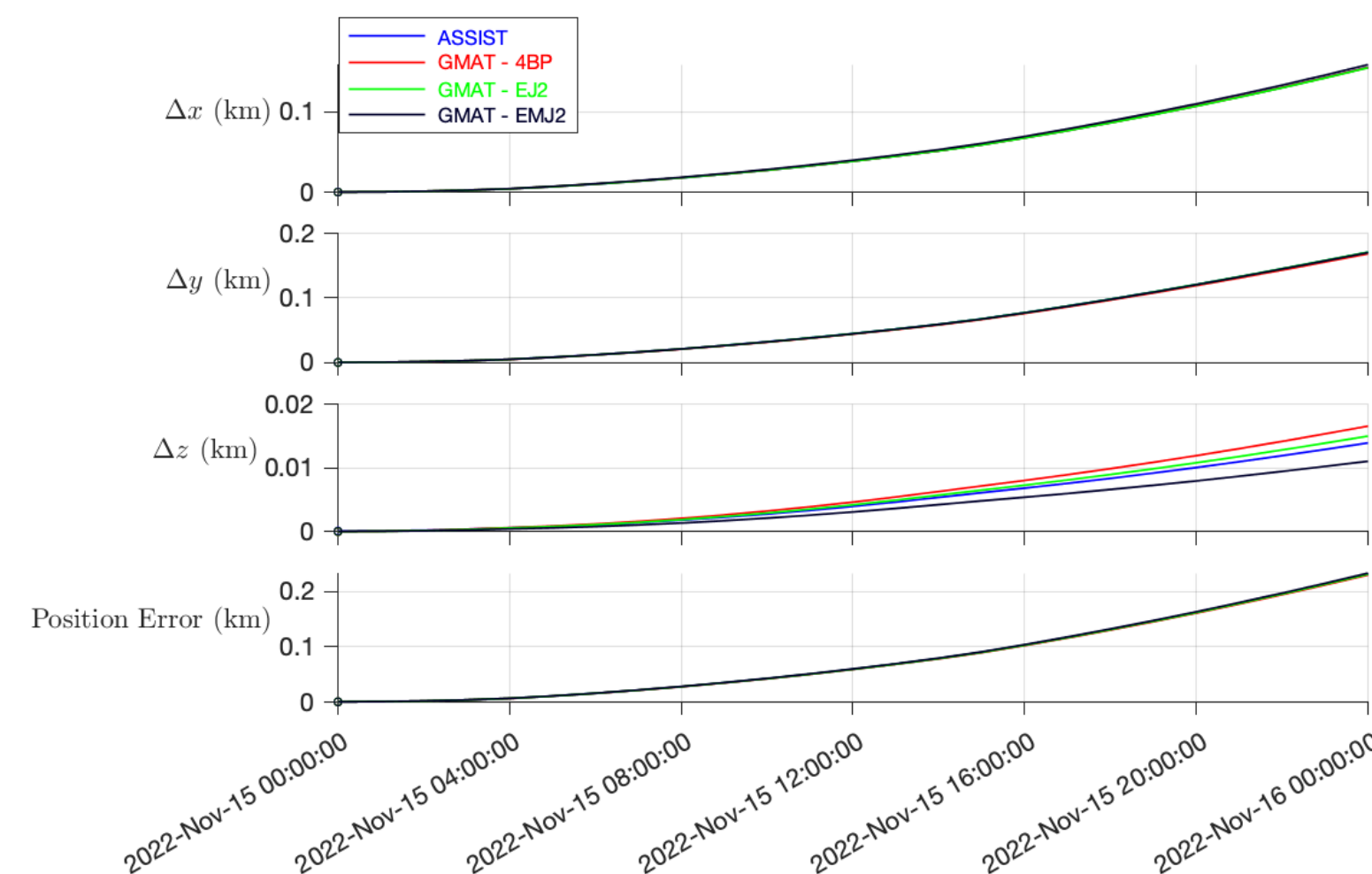




## Comparison of integration results to CAPSTONE ephemeris

### Preliminary test: 24-hr propagation period

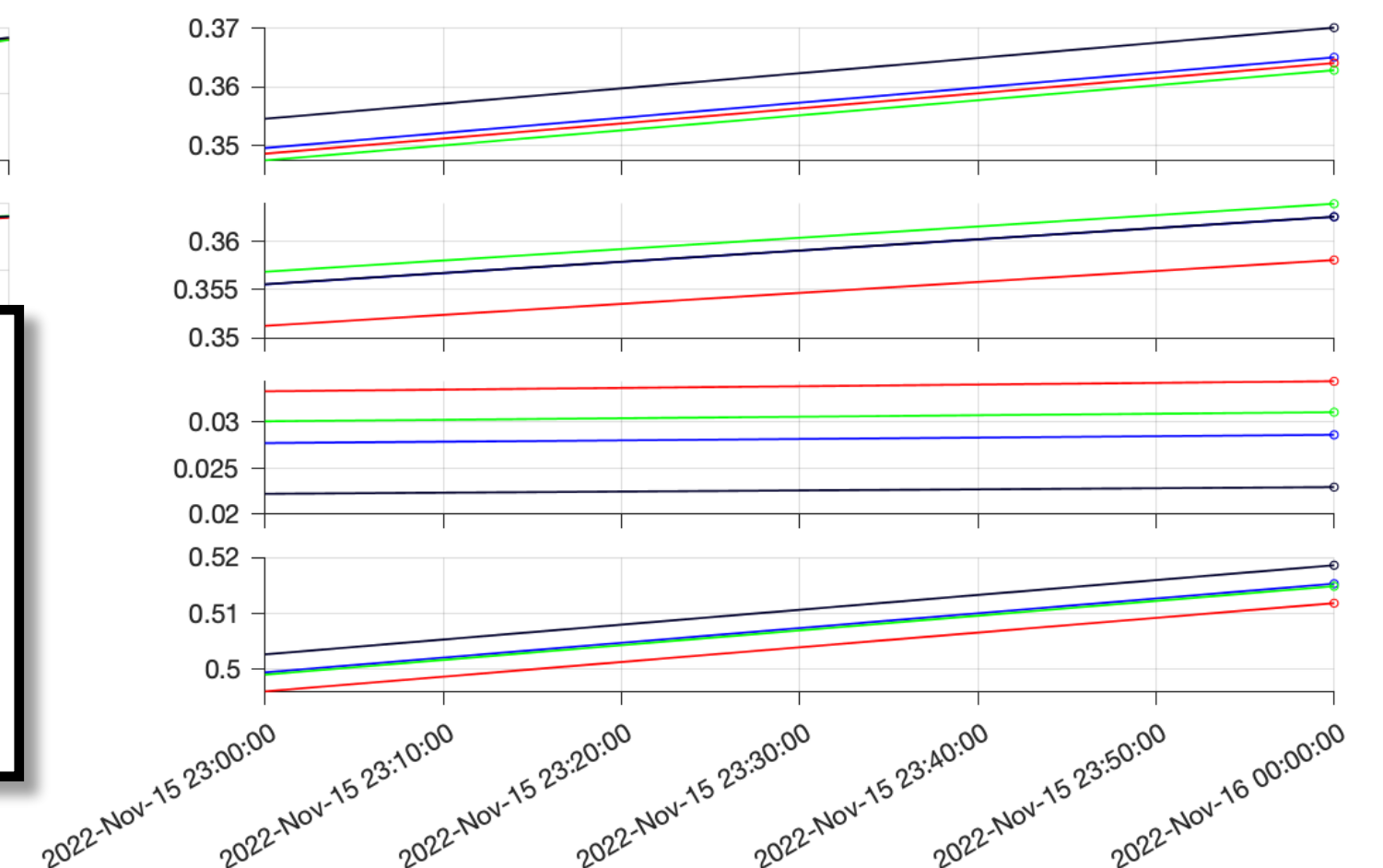
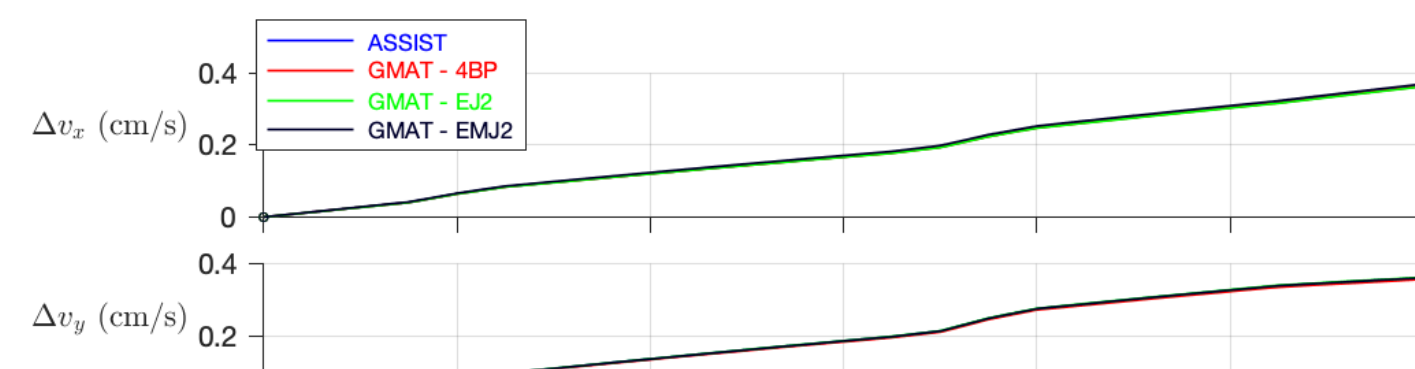
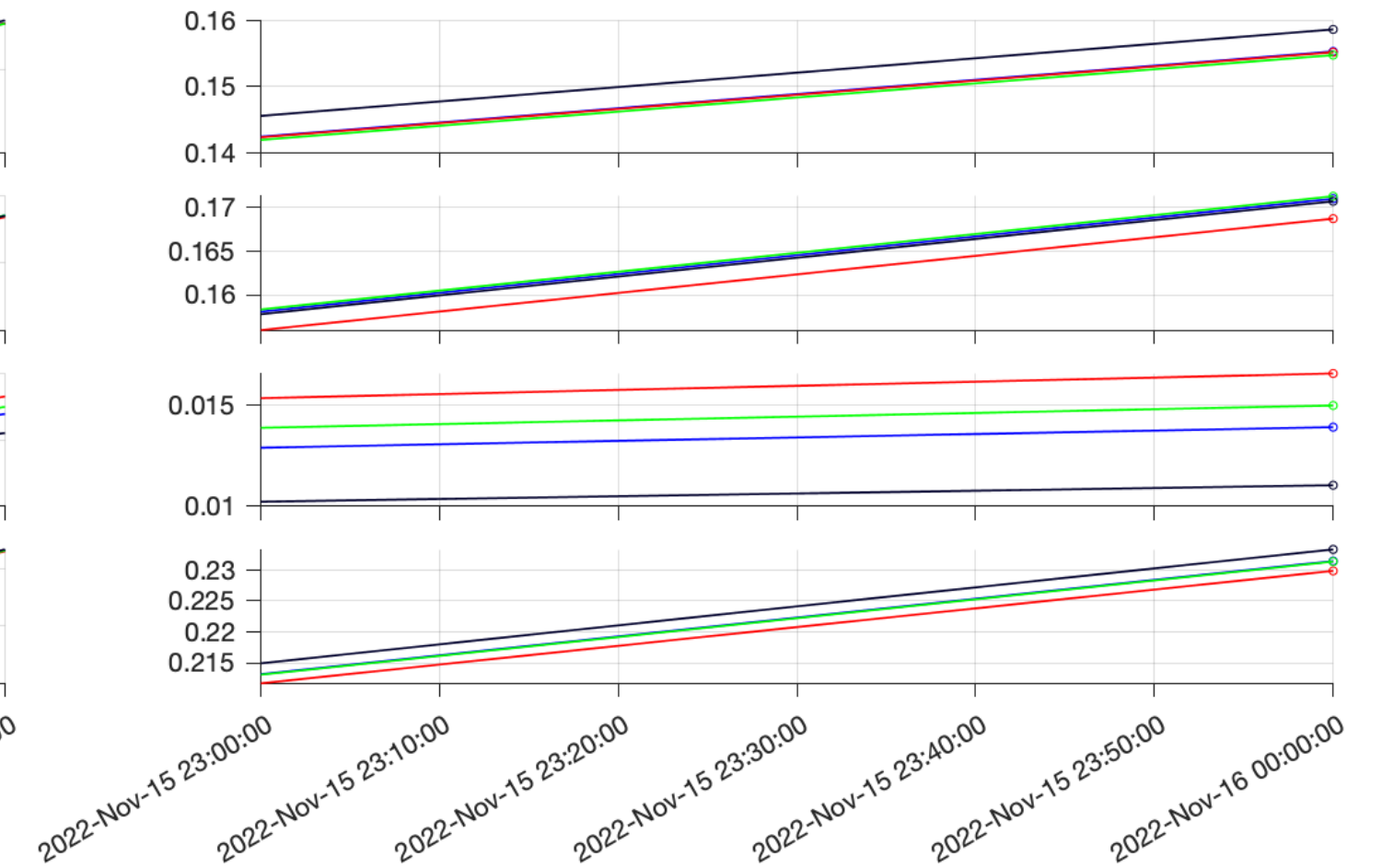
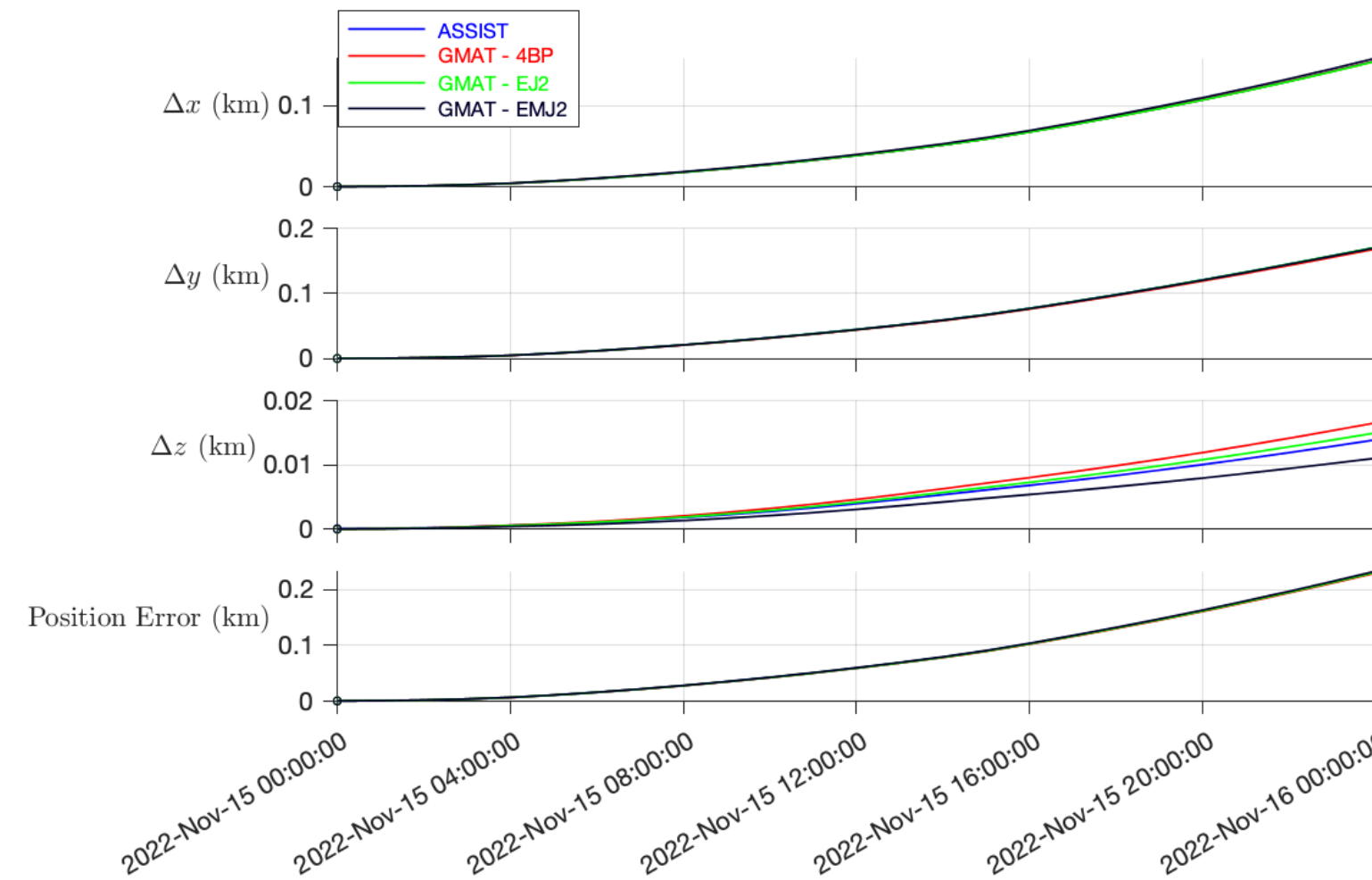
- Begin with initial conditions of CAPSTONE at an epoch (15 Nov 2022) provided by JPL Horizons
- Propagate using ASSIST/GMAT
  - ASSIST: Standard model
  - GMAT-4BP: Earth+Moon+Sun
  - GMAT-EJ2: All planets + Earth's  $J_2$
  - GMAT-EMJ2: GMAT-EJ2 + Moon's  $J_2$
- Compare propagated results with ephemeris at epochs



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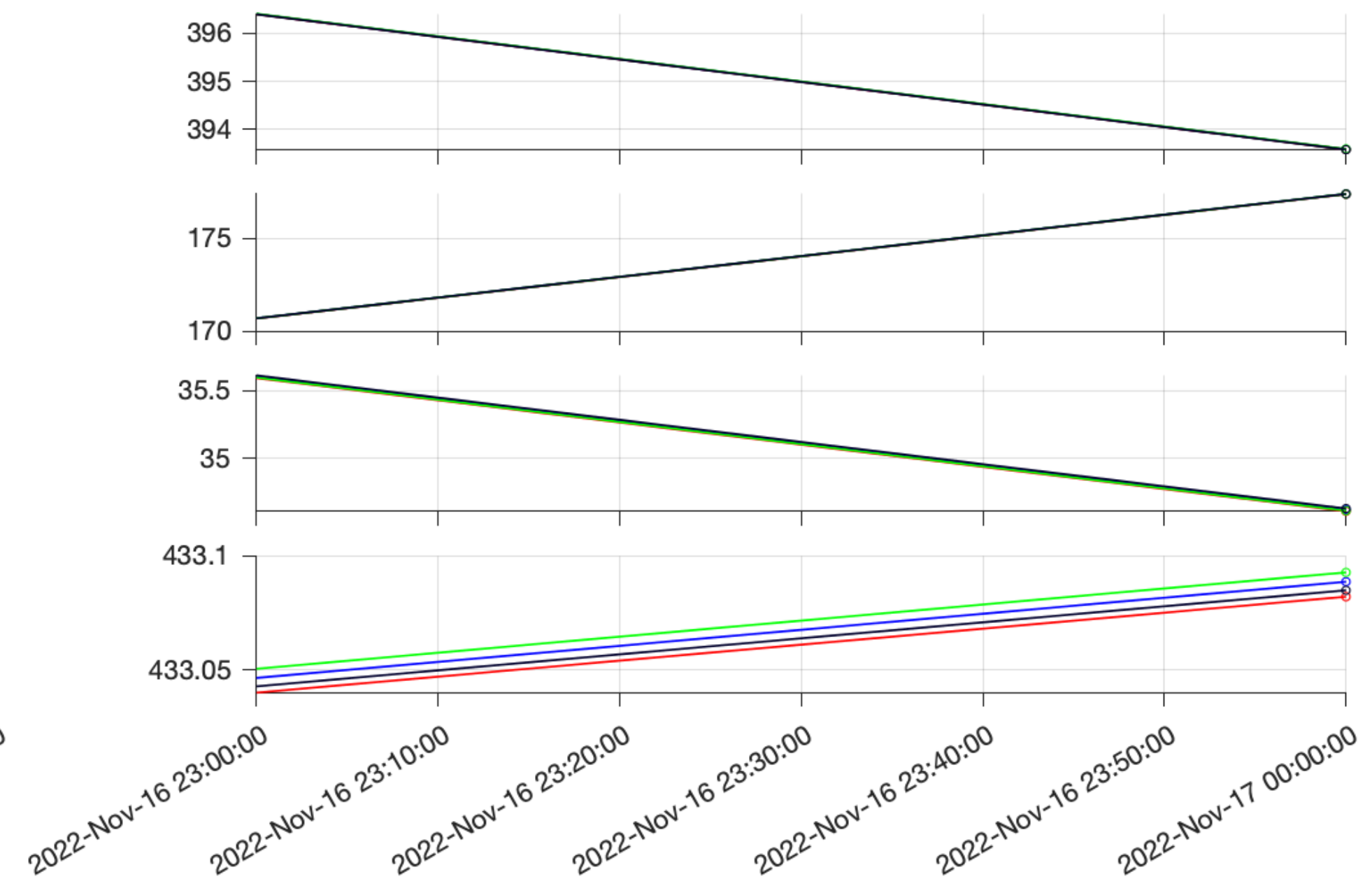
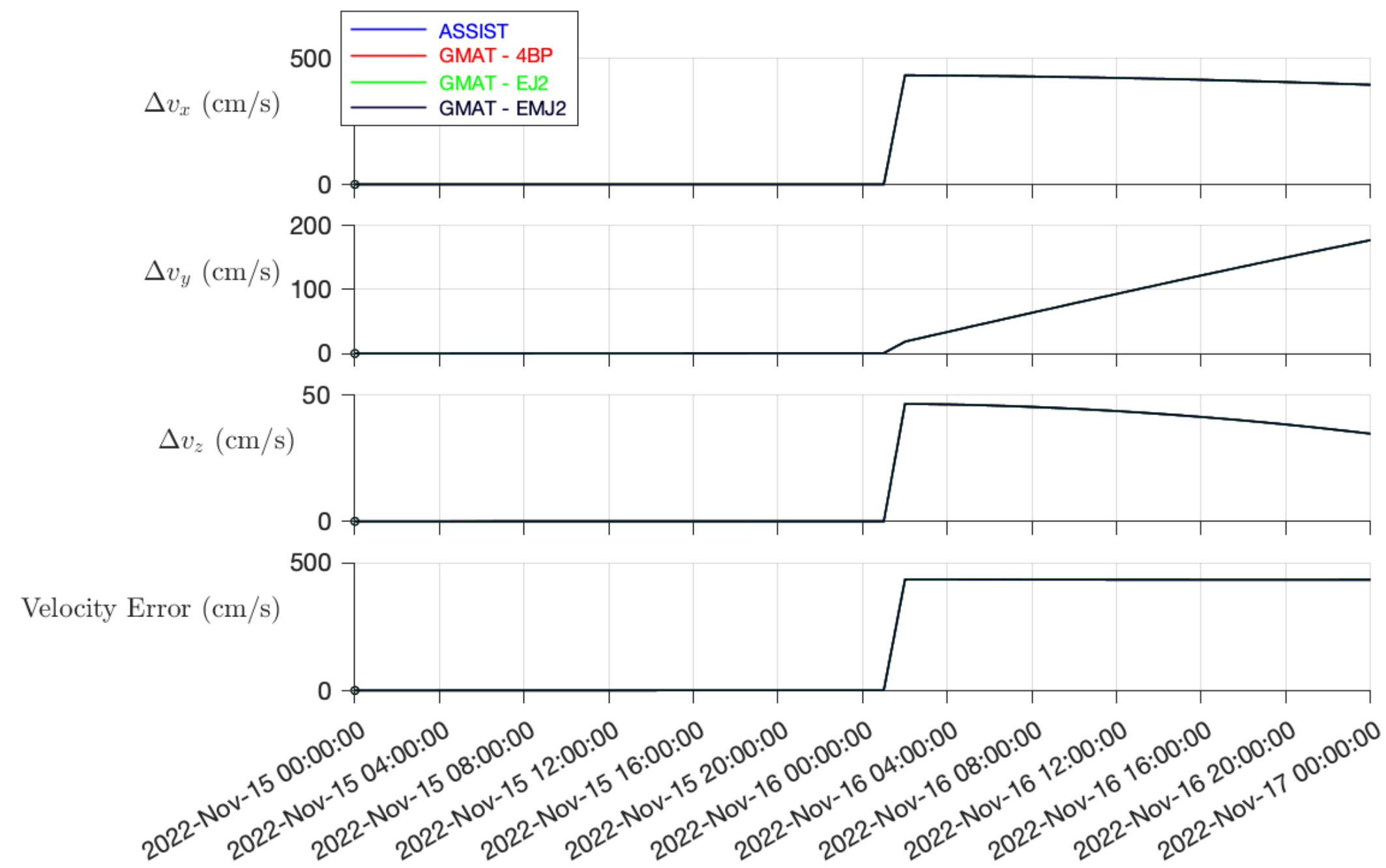
Model	ASSIST	GMAT-4BP	GMAT-EJ2	GMAT-EMJ2
Final Position Error (km)	0.22375	0.22222	0.22367	0.22557
Final Velocity Error (cm/s)	0.53015	0.52648	0.52956	0.53332



## Retrospective inspection of Cartesian residuals

- Numerical integrators only function as accurate approximations of the ephemeris during non-maneuvering periods
- CAPSTONE performs orbit maintenance maneuvers (OMMs) to maintain the NRHO
- Maneuvers (magnitude, direction, and epoch) are not explicitly stated in ephemeris repositories
- **Conclusion: ability to detect that a maneuver has occurred is a necessity for performing numerical integrator analysis**

### Retrospective Inspection of Velocity Error

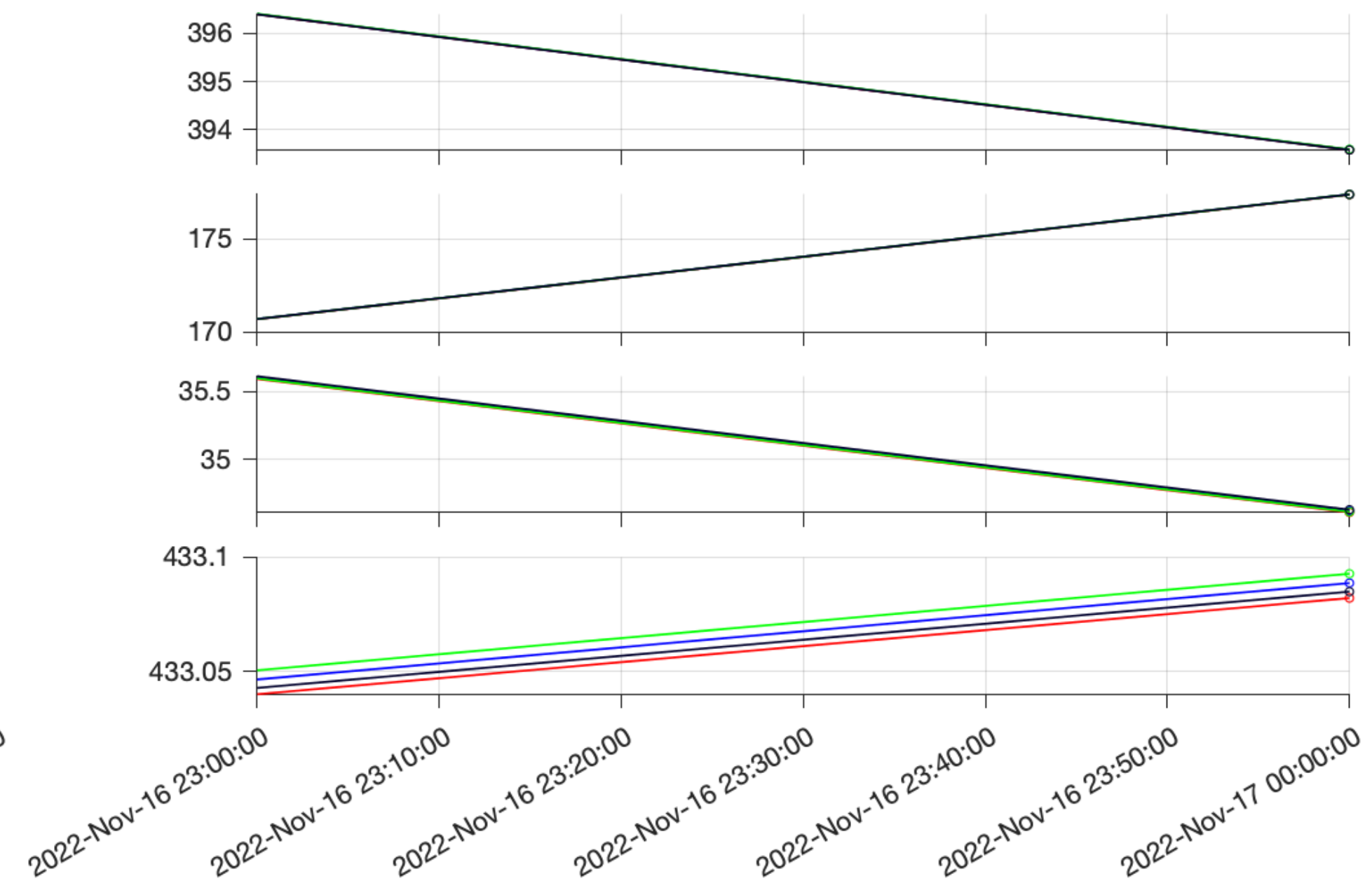
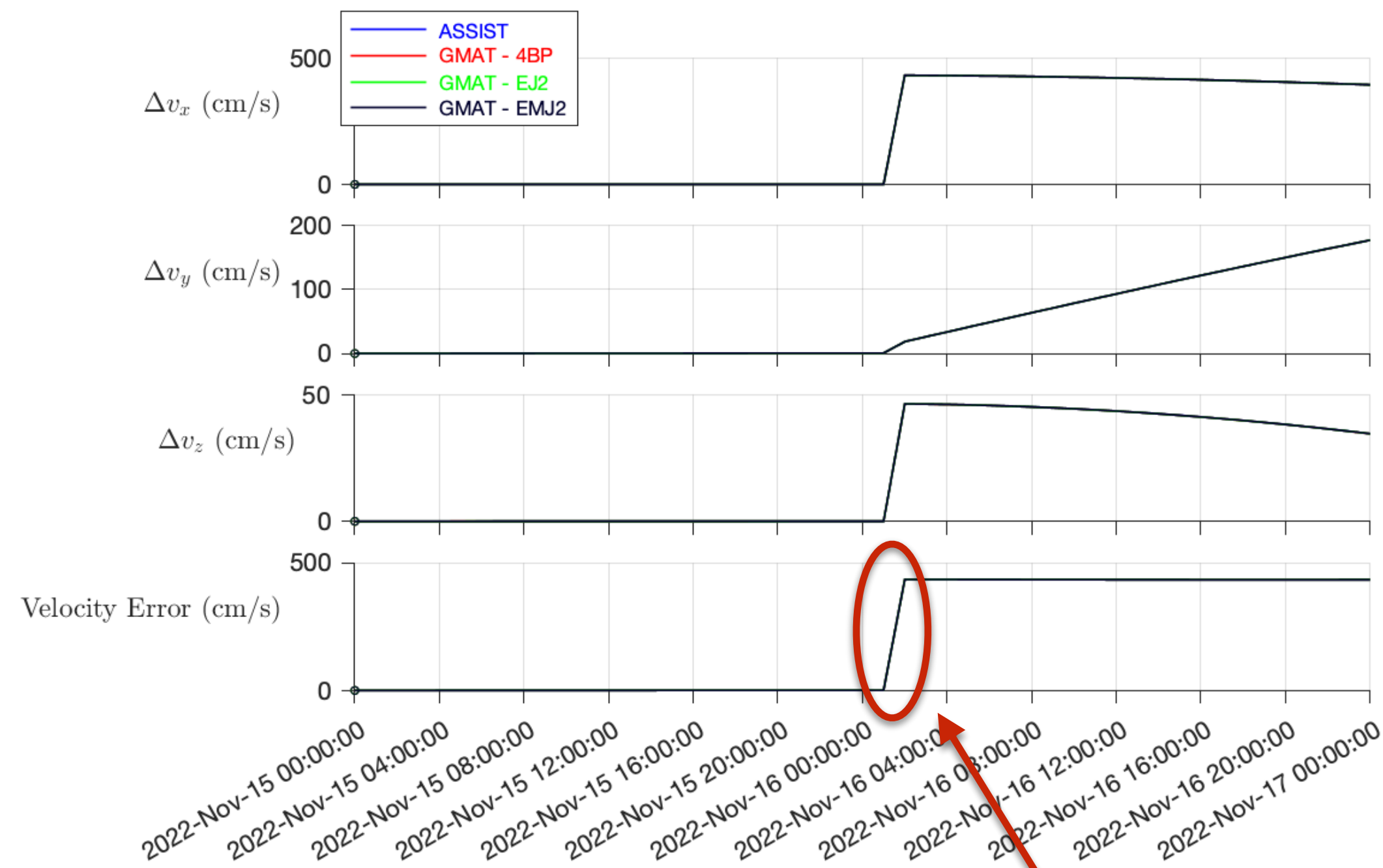




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### Retrospective Inspection of Velocity Error



**Instantaneous shift in velocity (indicative of a maneuver)**





## Inspection over longer propagation window

### • Procedure

1. Determine a propagation window wherein retrospective maneuver detection will be applied
  - 15 Nov 2022 - 01 Jan 2023 (insertion into NRHO to EOY)
2. Initialize numerical integration simulations every  $n$  hours throughout the entire propagation window from ICs provided by ephemeris
  - $n = 12$  hours, ephemeris step size = 1 hour
3. Propagate simulations through window
4. Retrospectively analyze for each simulation where

$$\text{velocity residual error}(t + \Delta t) - \text{velocity residual error}(t) > \text{threshold value}$$

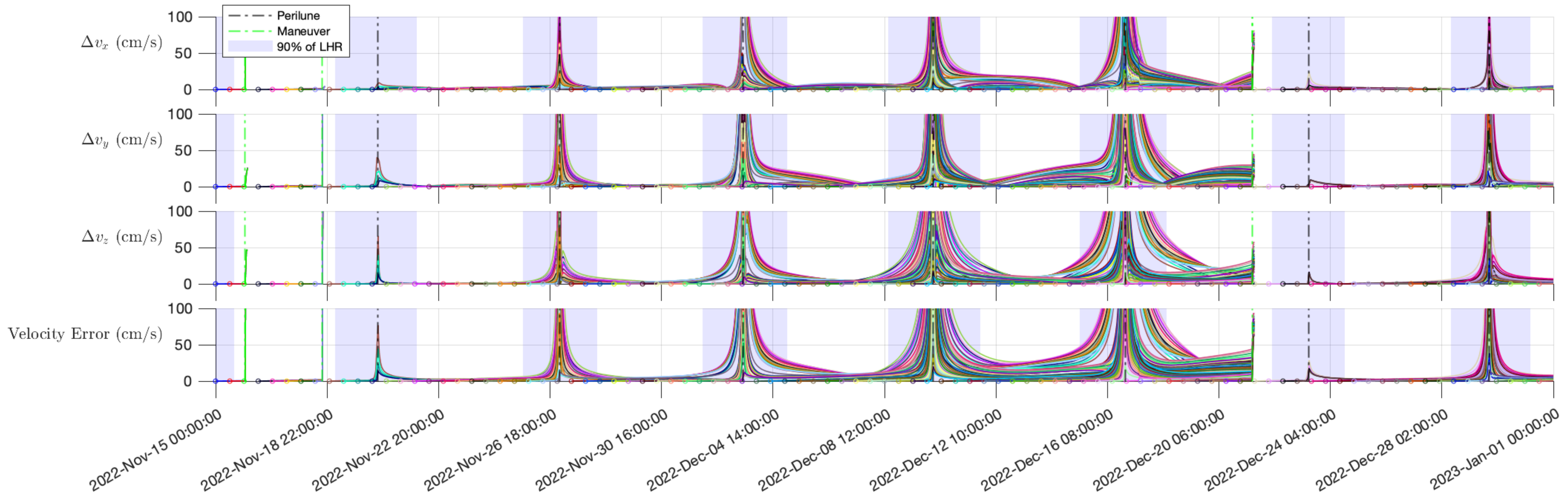
- threshold value = 5 cm/s (per Advanced Space, maneuvers have magnitudes from 5 to 50 cm/s)

### • Considerations

- Large shifts in velocity between time steps are expected near periselene as velocity increases
- Because of this, uncertainty of state estimation increases, thus Advanced Space has confirmed they do not perform OMMs “near periselene”
- **Solution: develop “no-go” zone where maneuver triggers are ignored, Lunar Hill Region (LHR)**

$$r_{LHR} = a_{\zeta} \left( \frac{m_{\zeta}}{3m_{\oplus}} \right)^{1/3}$$





## • Considerations: Complete Maneuver Detection Window - Velocity

- Large shifts in velocity between time steps are expected near periselene as velocity increases
- Because of this, uncertainty of state estimation increases, thus Advanced Space has confirmed they do not perform QMMs “near periselene”

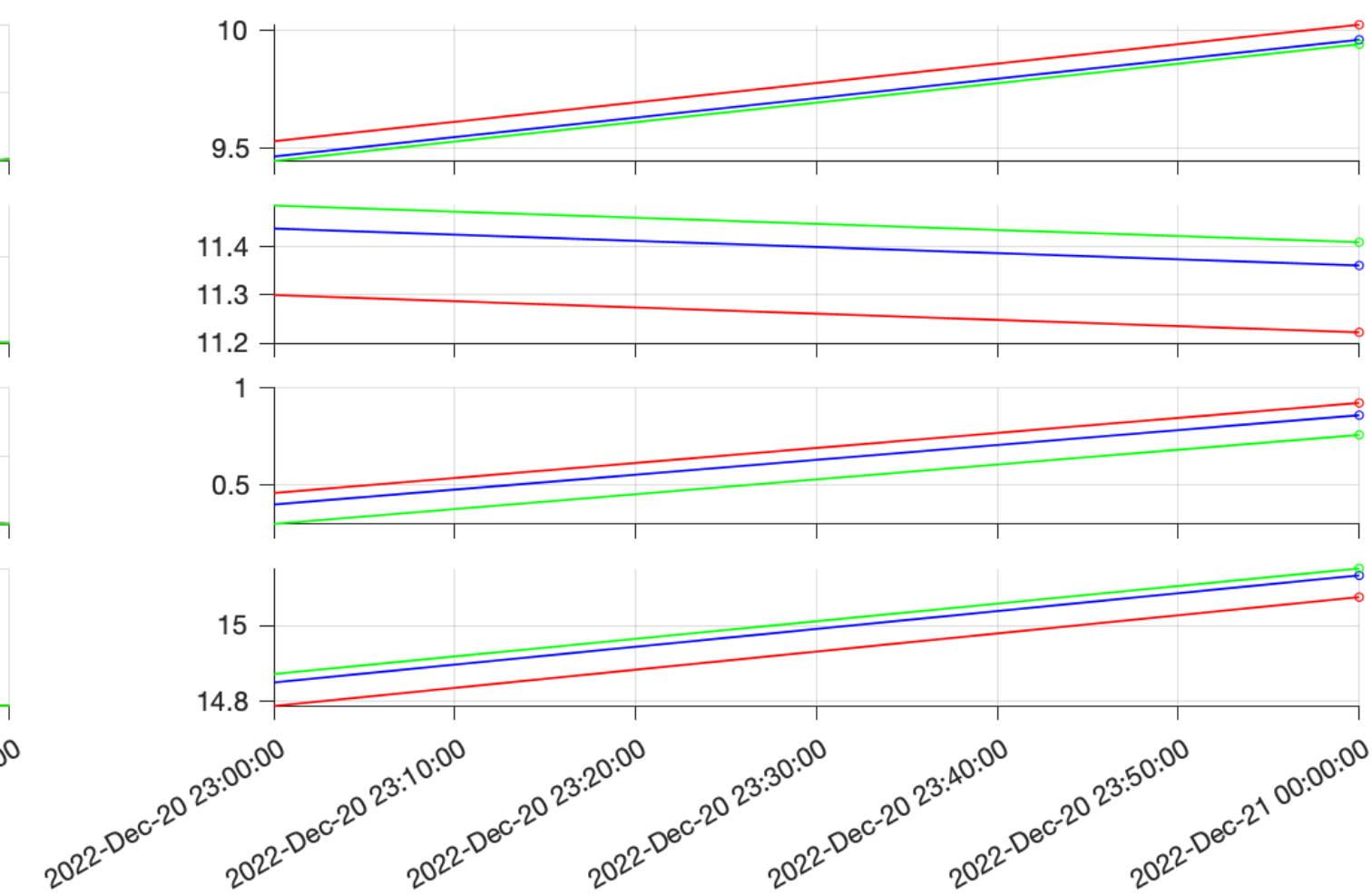
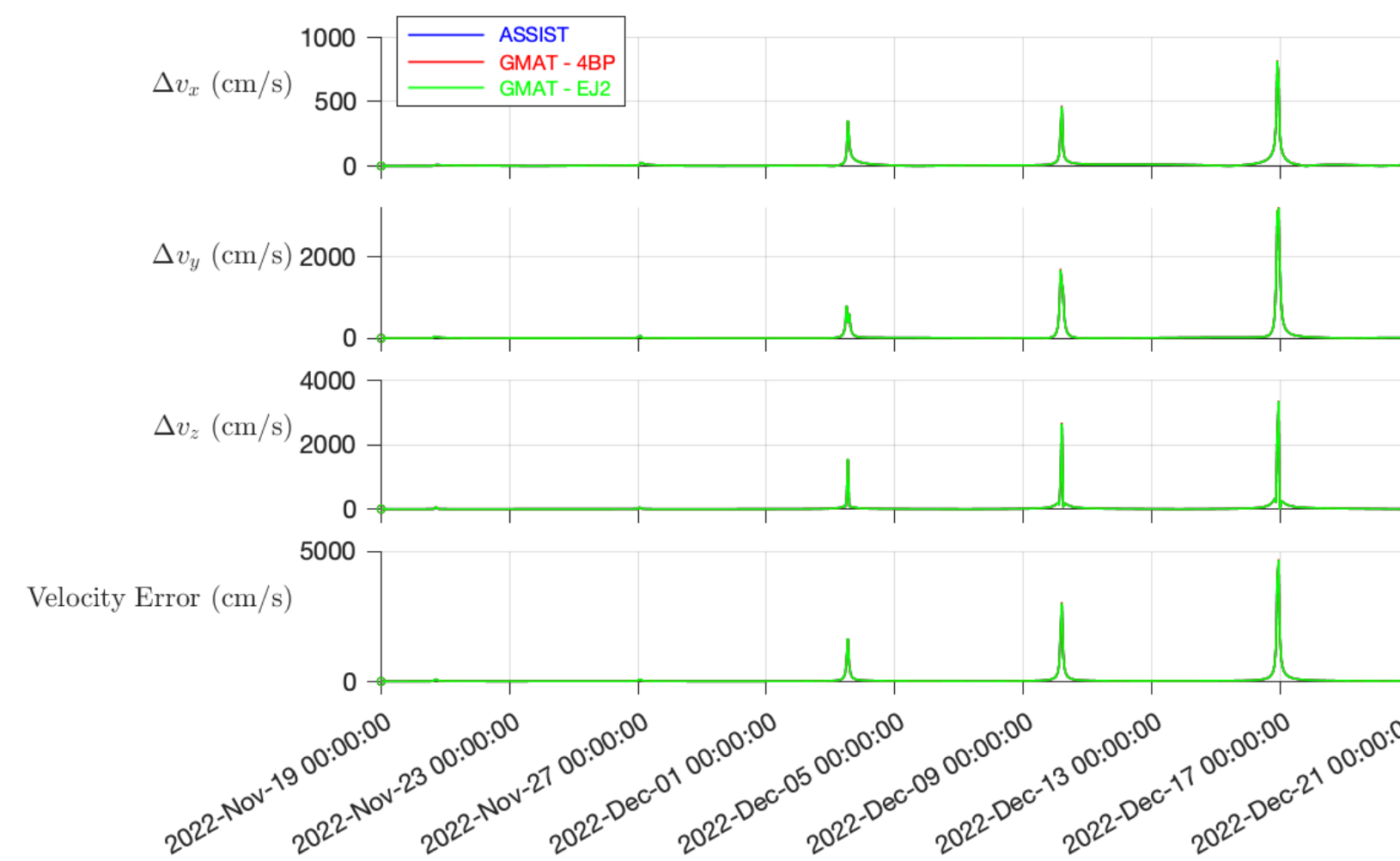
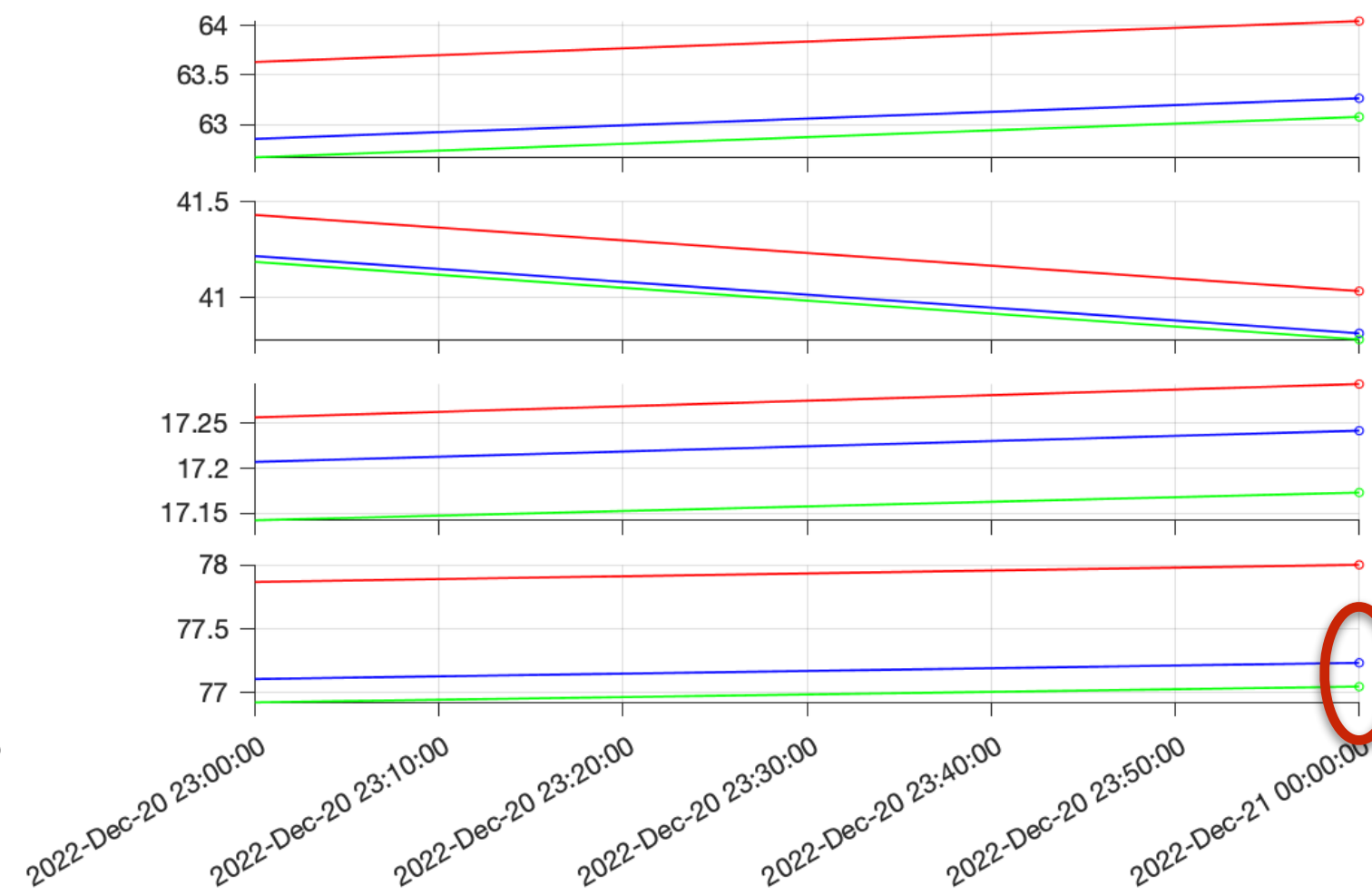
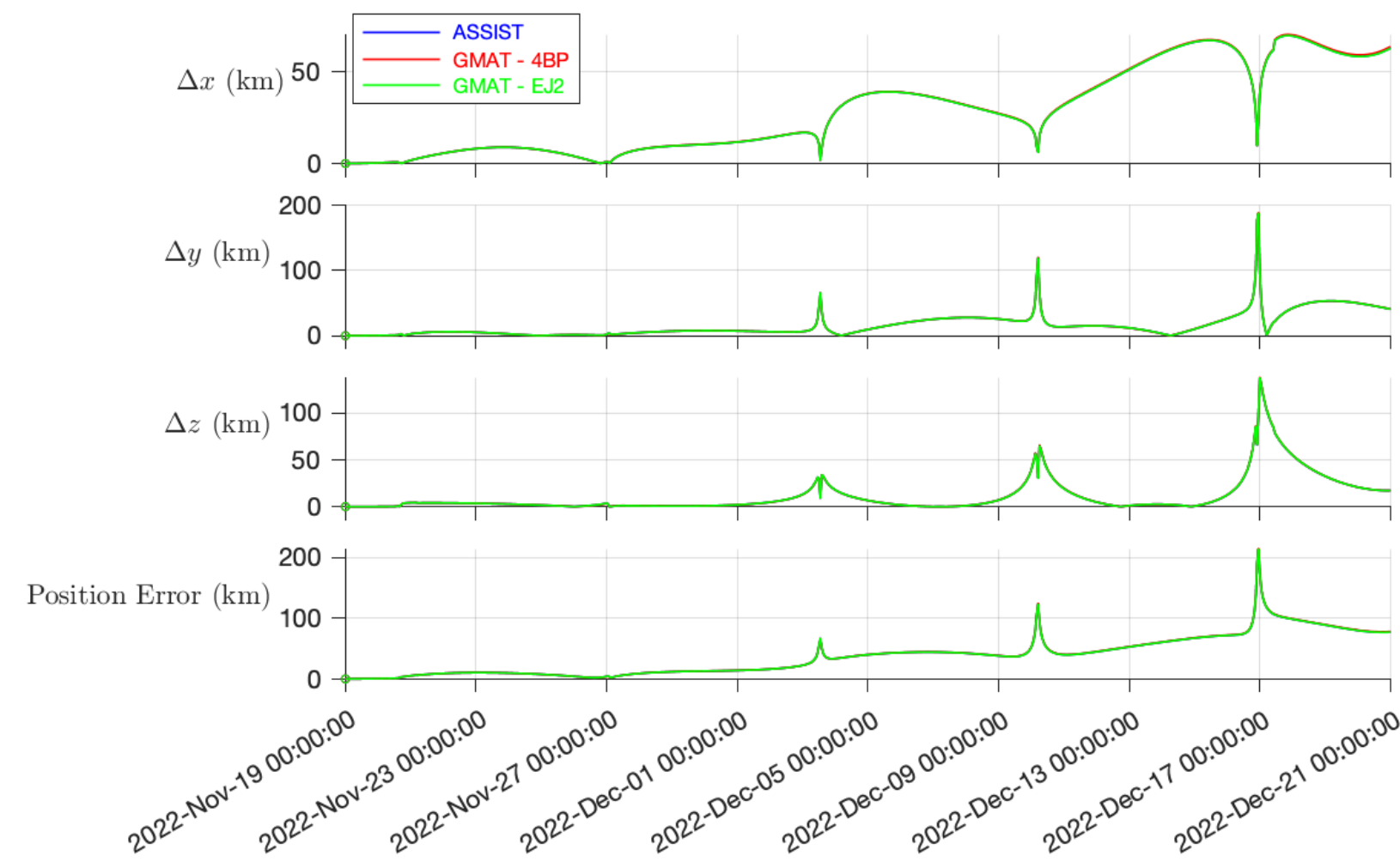
Maneuver Table

Maneuver #	Maneuver Date (UTC)	# of Triggers	Trigger Rate
1	16 Nov. 2022 01:00:00	3	100%
2	18 Nov. 2022 18:00:00	5	100%
3	21 Dec. 2022 10:00:00	65	100%

- Expected ~1 maneuver/week
- Maneuver threshold value may have been too high or no-go zone may be too large
- Carry-on with assumption that 19 Nov 2022 to 21 Dec 2022 is maneuver-free period



### Propagation window: 19 Nov 2022 00:00:00 UTC - 21 Dec 2022 00:00:00 UTC (32 days)



- ASSIST and GMAT-EJ2 are most accurate force models
- ASSIST includes  $J_2$  of the Sun, as well as other perturbations from asteroids that are most likely not included in the orbit determination model

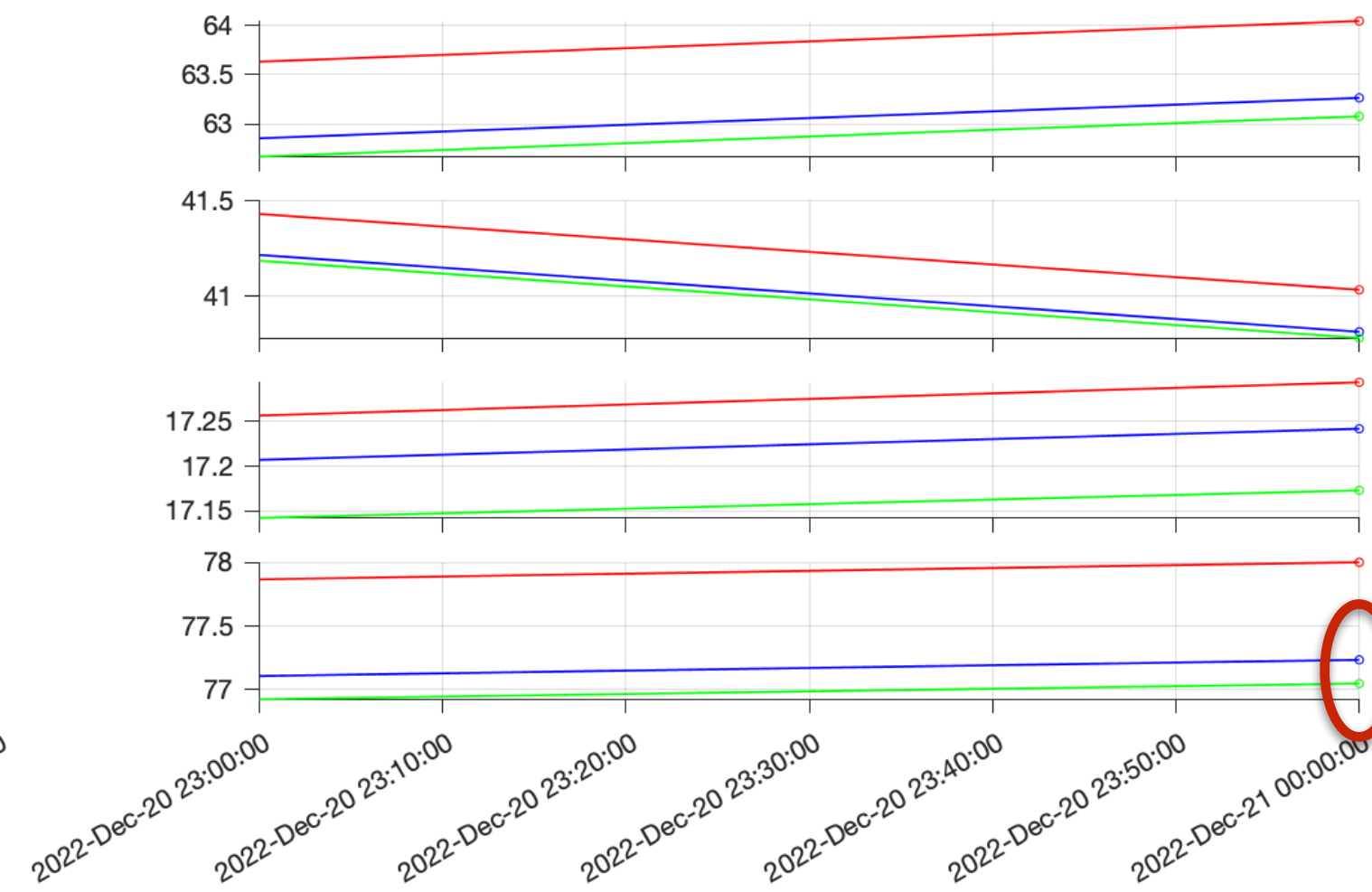
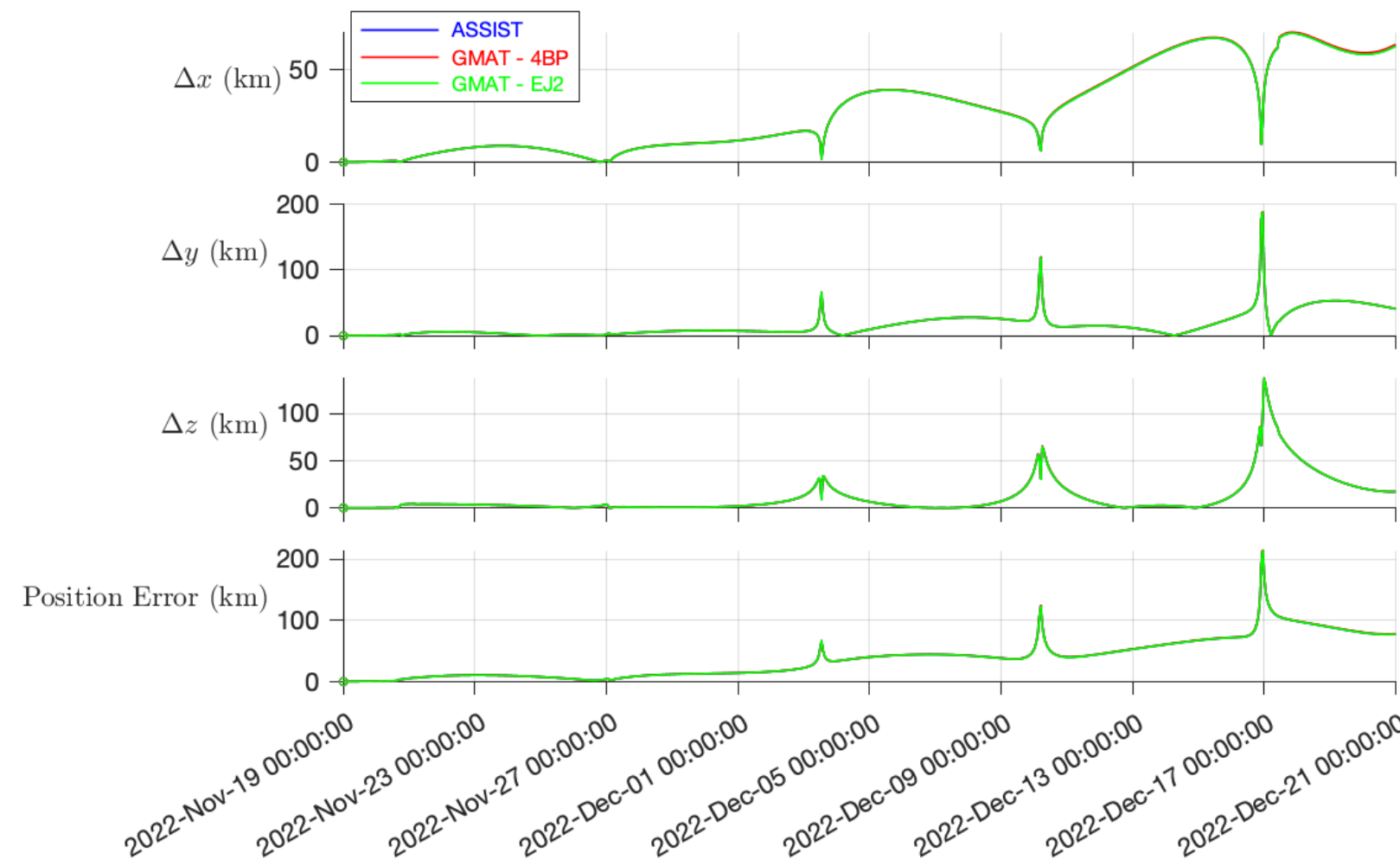




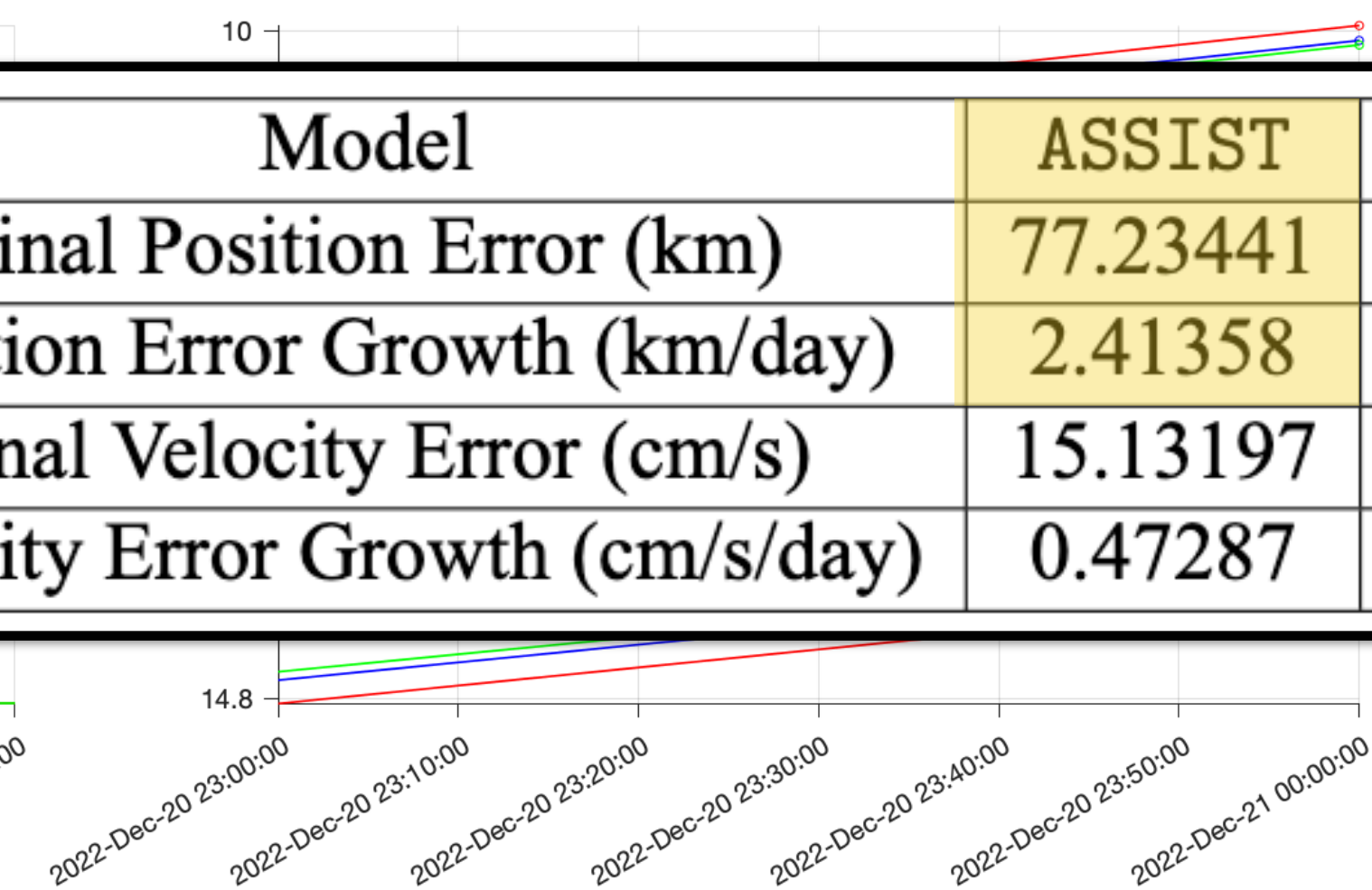
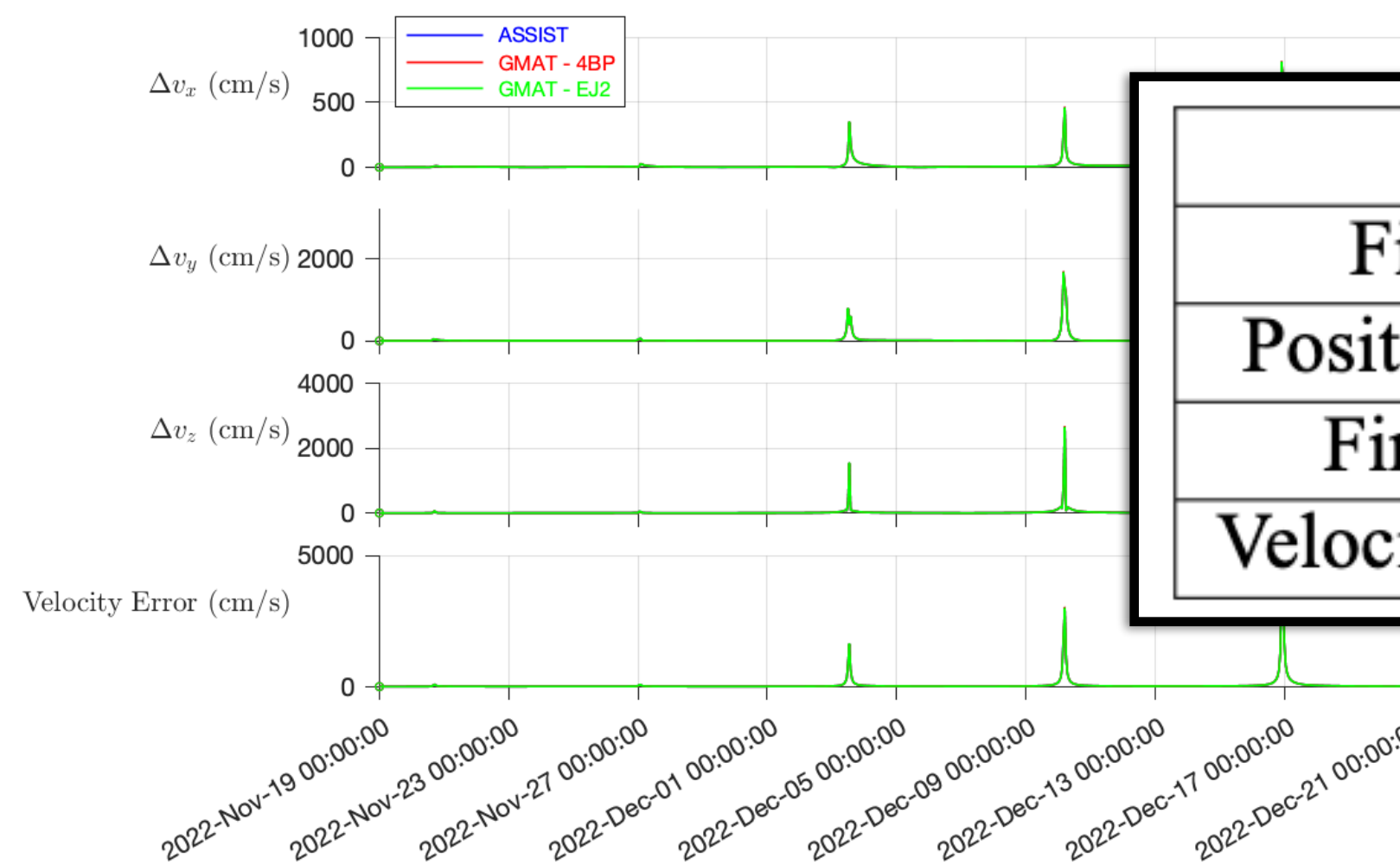
# Numerical Integrator Analysis

## Long term propagation period comparison

**Propagation window: 19 Nov 2022 00:00:00 UTC - 21 Dec 2022 00:00:00 UTC (32 days)**



- ASSIST and GMAT-EJ2 are most accurate force models
- ASSIST includes  $J_2$  of the Sun, as well as other perturbations from asteroids that are most likely not included in the orbit determination model



Model	ASSIST	GMAT-4BP	GMAT-EJ2	GMAT-EMJ2
Final Position Error (km)	77.23441	77.99987	77.04892	159.56883
Position Error Growth (km/day)	2.41358	2.43750	2.40778	4.98653
Final Velocity Error (cm/s)	15.13197	15.07480	15.15035	32.59955
Velocity Error Growth (cm/s/day)	0.47287	0.47109	0.47345	1.01874





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The authors would like to thank Patrick Miga and Bradley Cheetham from Advanced Space for their invaluable insight and contributions.

All code can be found at: <https://github.com/bhanson10/CAPSTONE> and [https://github.com/bhanson10/TESS\\_IBEX\\_Spektr-R](https://github.com/bhanson10/TESS_IBEX_Spektr-R).

Thank you for your time. Questions?